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Project: **Active Filter based on Conservative Power Theory (CPT) with digital controller.**
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Parameters Specifications

$V_{s_ef} := 127$ RMS grid phase-voltage

$f_s := 60$ Grid Frequency

$VDC := 220$ DC link Voltage

$L_f := 4.8 \cdot 10^{-3}$ Active Filter inductor output

$R_f := 0.1$ Active Filter resistance output

$H_i := 0.1$ Current Sensor Gains

$V_t := 1$ Carrier Amplitude

$F_s := 30 \cdot 10^3$ Switching Frequency

$f_c := \frac{F_s}{20} = 1.5 \times 10^3$ Desired cut-off frequency

$MF_d := 55$ Desired Margin Phase

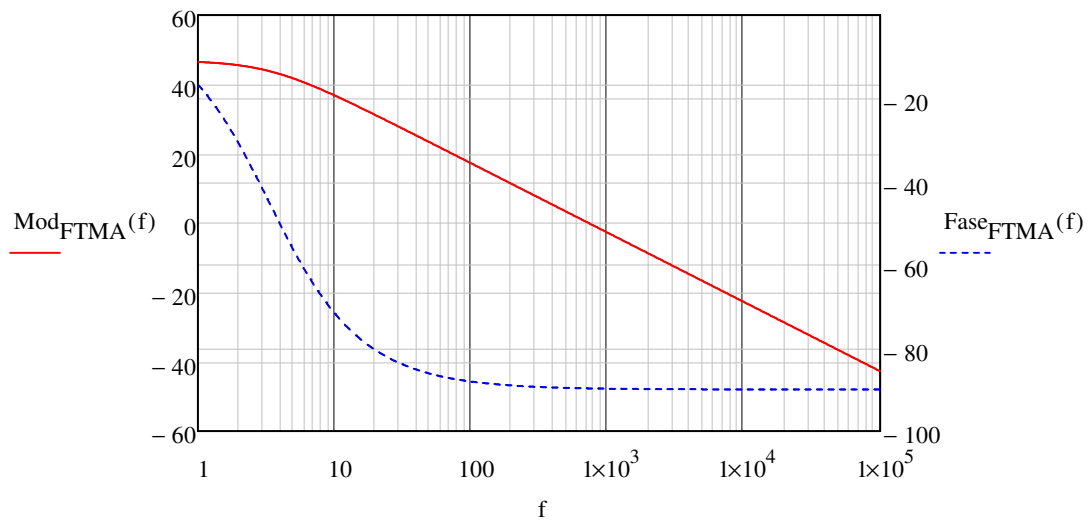
$T_a := \frac{1}{F_s} = 3.333333333333 \times 10^{-5}$ Switching period

$G_i(f) := \frac{VDC}{2 \cdot \pi \cdot f \cdot i \cdot L_f + R_f}$ Current Plant Gls(Z)

$FTMA(f) := H_i \cdot G_i(f)$

$Mod_{FTMA}(f) := 20 \cdot \log(|FTMA(f)|)$

$Fase_{FTMA}(f) := \arg(G_i(f)) \cdot \frac{180}{\pi}$



Controller Design

$$G_{c_dB} := \text{Mod}_{\text{FTMA}}(f_c)$$

$$G_{c_dB} = -6.261814899986 \quad \text{dB gain}$$

$$G_c := 10^{\frac{|G_{c_dB}|}{20}} \quad \text{Real gain to be compensated}$$

$$G_c = 2.056320215265$$

$$F_u := \text{Fase}_{\text{FTMA}}(f_c)$$

$$F_u = -89.87334872673$$

$$\alpha_2 := \text{MF}_d - F_u - 90 \quad \text{Required Phase [degree]}$$

$$\alpha_2 = 54.87334872673$$

$$K_2 := \tan\left(\frac{\alpha_2 \cdot \frac{\pi}{180}}{2} + \frac{\pi}{4}\right)$$

$$K_2 = 3.159414619832$$

$$\text{Prod}_2 := \frac{1}{2 \cdot \pi \cdot f_c \cdot G_c \cdot K_2} \quad \text{Prod}_2 = C_2 \cdot R_1$$

$$\text{Prod}_2 = 1.633170415287 \times 10^{-5}$$

$$C_2 := 100 \cdot 10^{-9} \quad \text{Adobted}$$

$$R_1 := \frac{\text{Prod}_2}{C_2}$$

$$R_1 = 163.317041528734$$

$$C_1 := C_2 \cdot (K_2^2 - 1)$$

$$C_1 = 8.981900740005 \times 10^{-7}$$

$$R_2 := \frac{K_2}{2 \cdot \pi \cdot f_c \cdot C_1}$$

$$R_2 = 373.222007663598$$

$$C_{\text{tipo2}}(f) := \frac{1 + 2\pi \cdot f \cdot i \cdot C_1 \cdot R_2}{2 \cdot \pi \cdot f \cdot i \cdot R_1 \cdot (C_1 + C_2 + 2 \cdot \pi \cdot f \cdot i \cdot R_2 \cdot C_1 \cdot C_2)} \quad \text{Type 2 controller transfer function}$$

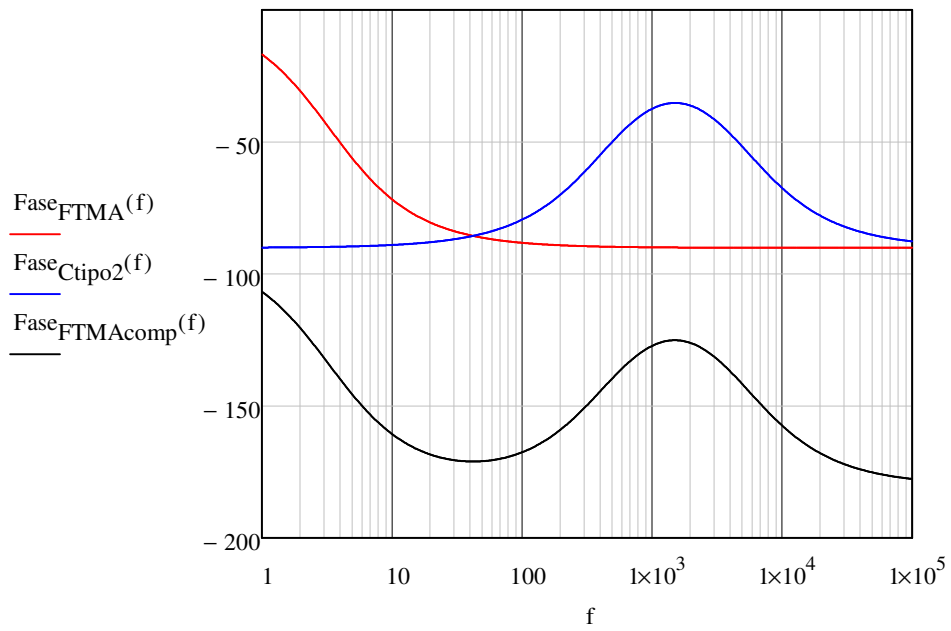
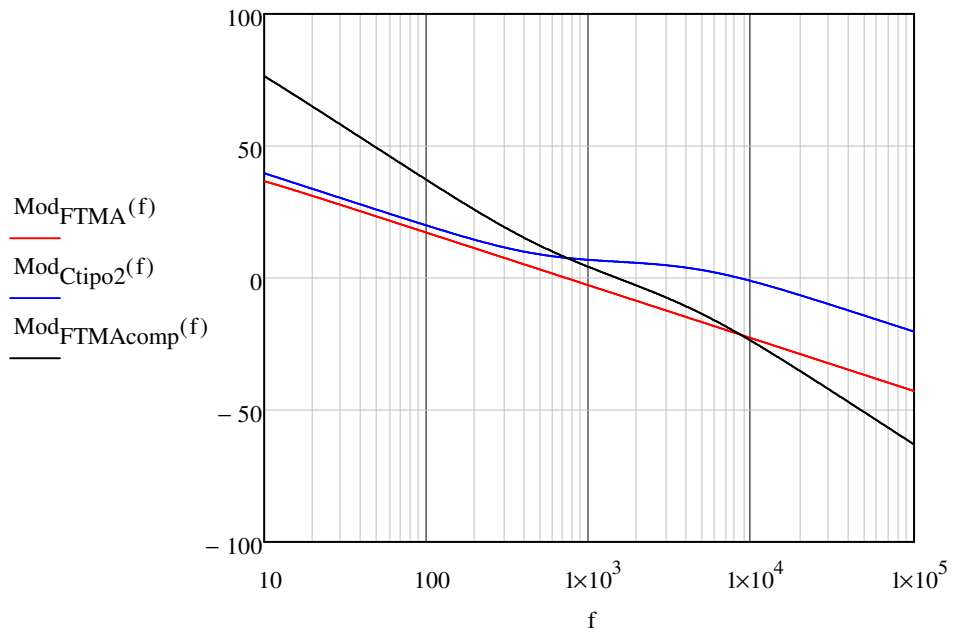
$$\text{Mod}_{C_{\text{tipo2}}}(f) := 20 \cdot \log(|C_{\text{tipo2}}(f)|)$$

$$\text{Fase}_{C_{\text{tipo2}}}(f) := \arg(C_{\text{tipo2}}(f)) \cdot \frac{180}{\pi}$$

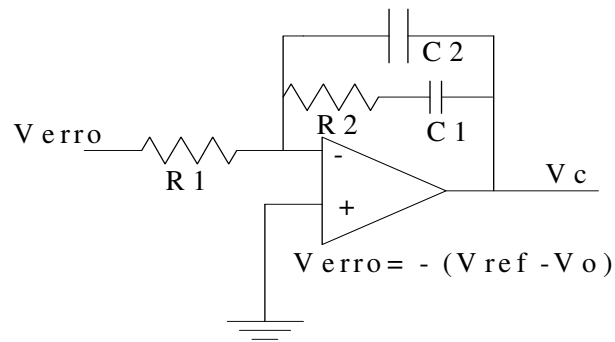
$$\text{FTMA}_{\text{comp}}(f) := \text{FTMA}(f) \cdot C_{\text{tipo2}}(f) \quad \text{Open-loop transfer function}$$

$$\text{Mod}_{\text{FTMA}_{\text{comp}}}(f) := 20 \cdot \log(|\text{FTMA}_{\text{comp}}(f)|)$$

$$\text{Fase}_{\text{FTMA}_{\text{comp}}}(f) := \arg(\text{FTMA}_{\text{comp}}(f)) \cdot \frac{180}{\pi}$$



Implementation



$$R_1 = 163.317041528734 \quad C_1 = 8.981900740005 \times 10^{-7}$$

$$R_2 = 373.222007663598 \quad C_2 = 1 \times 10^{-7}$$

Digital: z transfer function. PSIM implementation Cls(Z)

$$\beta := 4 \cdot R_1 \cdot R_2 \cdot C_1 \cdot C_2 + 2 \cdot T_a \cdot R_1 \cdot (C_1 + C_2) = 3.27672331963 \times 10^{-8}$$

Numerator coefficients

$$b_0 := \frac{T_a^2 + 2 \cdot T_a \cdot C_1 \cdot R_2}{\beta} = 0.715940763629$$

$$b_1 := \frac{2 \cdot T_a^2}{\beta} = 0.067818427296$$

$$b_2 := \frac{T_a^2 - 2 \cdot T_a \cdot C_1 \cdot R_2}{\beta} = -0.648122336333$$

Denominator Coefficients

$$a_{\text{zero}} := 1$$

$$a_1 := \frac{-8 \cdot R_1 \cdot R_2 \cdot C_1 \cdot C_2}{\beta} = -1.336648499666$$

$$a_2 := \frac{4 \cdot R_1 \cdot R_2 \cdot C_1 \cdot C_2 - 2 \cdot T_a \cdot R_1 \cdot (C_1 + C_2)}{\beta} = 0.336648499666$$